

# Abduction



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# Automatic Reasoning

## Outline

$$\begin{array}{l} A \rightarrow B \\ A \end{array}$$

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$$B$$
$$\begin{array}{l} A \rightarrow B \\ A \end{array}$$

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$$?$$

Deduction

$$\begin{array}{l} ? \\ A \end{array}$$

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$$B$$

Induction

$$\begin{array}{l} A \rightarrow B \\ ? \end{array}$$

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$$B$$

Abduction

# Abduction

- We assume A because it explains B ...
- Abduction is inference to the **best explanation**
- Has applications to diagnosis, plan recognition, natural language understanding, vision, and many other tasks.
- It is frequently formalized as constructing a set of assumptions that logically imply and therefore "explain" a set of observations.
- The process of finding the best explanation from a set of observations
- First used by C. S. Pierce (1955)

# Abduction

- Abductive reasoning starts when an inquirer considers a set of seemingly unrelated facts, armed with the intuition that they are somehow connected
- Abduction is the process of inference that produces a hypothesis
  - Formation of plausible hypothesis
  - Selection of the best one

# Abduction

- Given:
  - Background knowledge KB
  - Observations O
- Find:
  - Hypothesis H such that
    - $KB \cup H \not\vdash \perp$
    - $KB \cup H \vdash O$
- Multiple hypothesis H !
  - That explain O given KB
  - Usually depends on
    - the size (or simplicity) of H
    - the coherence of H (selects H that maximally connects O)

# Abduction

- Abduction or Inference to the Best Explanation is a form of inference that follows a pattern like this:
  - D is a collection of data (facts, observations, givens),
  - H explains D (would, if true, explain D),
  - No other hypothesis explains D as well as H does.

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- Therefore, H is probably correct.

# Abduction

- Extreme example of abduction from Eugene Ionesco's play “Rhinoceros” from the “Theater of the Absurd” school:
  - All cats die.
  - Socrates is dead.
  - Therefore, Socrates is a cat.

# Abduction

- Textual Entailment (Recognizing Textual Entailment task, RTE)
  - T entails H, H is a consequent of T,  $T \Rightarrow H$ 
    - Directional relationship between a coherent text T and H
    - If the meaning of H, as interpreted in the context of T, can be inferred from the meaning of T, as would typically be interpreted by people
  - T: Peter brings his car to the garage for repair
  - H: Peter's car is damaged
  - $T \Rightarrow H$
  - T: Corrosion caused intermittent electrical contact
  - H: Corrosion prevented continuous electrical contact
  - $T \Rightarrow H$
  - T: Marlowe opened the refrigerator
  - H: Marlowe was hungry
  - $T \Rightarrow H$



# Abduction

- The strength of an abductive conclusion will in general depend on several factors, including:
  - how good H is by itself
    - independently of considering the alternatives
  - how decisively H surpasses the alternatives
  - how exhaustive the search was for alternative explanations, and
  - pragmatic considerations, including
    - the costs of being wrong and the benefits of being right,
    - how strong the need is to come to a conclusion at all, especially considering the possibility of seeking further evidence before deciding.

# Abduction

- FOL based approaches to abduction
  - Determine the set of assumptions sufficient to deduce the observations
    - Unable to reason under uncertainty
    - Unable to estimate the likelihood of alternative explanations
- Bayesian Networks
  - KB is encoded as a directed graph
  - Given  $O$  probabilistic inference over the graph is done to compute the posterior probability of alternative explanations
    - Essentially Propositional Logic
    - Cannot handle structured representations
- Weighted abduction, TACITUS (Hobbs et al. 1993)
  - Finds the lowest weight explanation
  - No solid theoretical basis

# Abduction

- Abduction using Markov Logic Networks (MLN)
  - (Kate & Mooney 2009)
  - Markov Logic Networks (Richardson & Domingos 2006)
  - Alchemy !
    - <http://alchemy.cs.washington.edu/>
  - Traditional FOL can be seen as hard constraints (0% vs. 100%)
  - MLN assigns a weight to each formula
  - The weight reflects how strong a constraint is
  - MLN is inherently deductive
  - MLN do not directly support abductive inference

# Abduction

*rained*  $\Rightarrow$  *grass\_is\_wet*

*sprinkler\_was\_on*  $\Rightarrow$  *grass\_is\_wet*

- Observations:

*grass\_is\_wet*

- Adding reverse implications

*grass\_is\_wet*  $\Rightarrow$  *rained*

*grass\_is\_wet*  $\Rightarrow$  *sprinkler\_was\_on*

- Abductive inference by deduction ...

*sprinkler\_was\_on*  $\sim >$  *grass\_is\_wet*  $\sim >$  *rained* (!)

- Both cannot be true ...

*grass\_is\_wet*  $\Rightarrow$   $\neg$  *rained*  $\vee$   $\neg$  *sprinkler\_was\_on*

# Abduction

$\forall X \forall Y (\text{mosquito}(X) \wedge \text{infected}(X, \text{malaria}) \wedge \text{bite}(X, Y) \Rightarrow \text{infected}(Y, \text{malaria}))$

$\forall X \forall Y (\text{infected}(X, \text{malaria}) \wedge \text{transfuse}(\text{blood}, X, Y) \Rightarrow \text{infected}(Y, \text{malaria}))$

- Observations:

$\text{infected}(\text{john}, \text{malaria})$

$\text{transfuse}(\text{blood}, \text{mary}, \text{john})$

- MLNs do not directly support abductive inference
- In MLNs we need to explicitly include clauses with reverse implications

# Abduction

$\forall X \forall Y (\text{mosquito}(X) \wedge \text{infected}(X, \text{malaria}) \wedge \text{bite}(X, Y) \Rightarrow \text{infected}(Y, \text{malaria}))$

Reverse implication:

$\forall Y (\text{infected}(Y, \text{malaria}) \Rightarrow \exists X (\text{mosquito}(X) \wedge \text{infected}(X, \text{malaria}) \wedge \text{bite}(X, Y)))$

$\forall X \forall Y (\text{infected}(X, \text{malaria}) \wedge \text{transfuse}(\text{blood}, X, Y) \Rightarrow \text{infected}(Y, \text{malaria}))$

Reverse implication:

$\forall Y (\text{infected}(Y, \text{malaria}) \Rightarrow \exists X (\text{infected}(X, \text{malaria}) \wedge \text{transfuse}(\text{blood}, X, Y)))$

If Y is infected with malaria then at least one of the possible explanations must be true:

$\forall Y (\text{infected}(Y, \text{malaria}) \Rightarrow$   
 $(\exists X (\text{mosquito}(X) \wedge \text{infected}(X, \text{malaria}) \wedge \text{bite}(X, Y))) \vee$   
 $(\exists X (\text{infected}(X, \text{malaria}) \wedge \text{transfuse}(\text{blood}, X, Y))))$

But both explanations cannot be true:

$\forall Y (\text{infected}(Y, \text{malaria}) \Rightarrow$   
 $\neg (\exists X (\text{mosquito}(X) \wedge \text{infected}(X, \text{malaria}) \wedge \text{bite}(X, Y))) \vee$   
 $\neg (\exists X (\text{infected}(X, \text{malaria}) \wedge \text{transfuse}(\text{blood}, X, Y))))$

# Abduction

- The Boston office called.
- There is an office “in” Boston (city)
- Somebody (person) works for/at the office
- The “in” relation can be expressed by a compound nominal
- An organization can play the role of the persons working for it

# Abduction



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